

Chapter 7 Acids & Bases

第七章 酸與鹼

Jwu-Ting Chen 陳竹亭

***Department of Chemistry, National Taiwan University
Taipei, Taiwan 106, jtchen@ntu.edu.tw***

➤ **What is acid? What is base?**

何謂酸？何謂鹼？

➤ **Are acids and bases two classes of substances that have opposite properties, and their character could be canceled off by meeting each other?**

酸與鹼是兩種性質相反的物質，相遇時彼此的性質就相互抵銷嗎？

Background 酸鹼的歷史

● *By tastes* 感官的認識

■ *Acids are a class of substances that taste sour*
酸嚐起來是「酸」的

■ *Bases (alkalis) are a class of substances that taste bitter*
鹼嚐起來是「苦」的

● *By Alchemist Experience*

煉金術士對酸與鹼的認識

■ *HCl was called salt spirit* HCl稱作鹽精

■ *Many metal containing minerals gave alkalis in water*
許多含金屬的礦物在水中呈現鹼性

■ *Minerals without metal often give acidic solutions*
許多不含金屬的礦物在水中呈現酸性

能舉例嗎？

● *Arrhenius concept – The First Modern Theory*

阿瑞尼士理論 1884

■ *Acids produce hydrogen ion in aqueous solutions*

酸在水溶液中產生氫離子(H^+)

■ *Bases produce hydroxide ion in aqueous solutions*

鹼在水溶液中產生氫氧根離子(OH^-)

● *The Content of Arrhenius Concept*

阿瑞尼士理論的精義

■ *Theory of Ionization* 游離說



■ *Electrolytes & Non-electrolytes*

電解質與非電解質

● *Brønsted-Lowry concept*

布忍司特—羅瑞理論

■ *Acid is proton donor in aqueous solution*

酸在水溶液中是質子供給者

■ *Base is proton acceptor in aqueous solution*

鹼在水溶液中是質子接受者

■ *Conjugate acid-base pair*

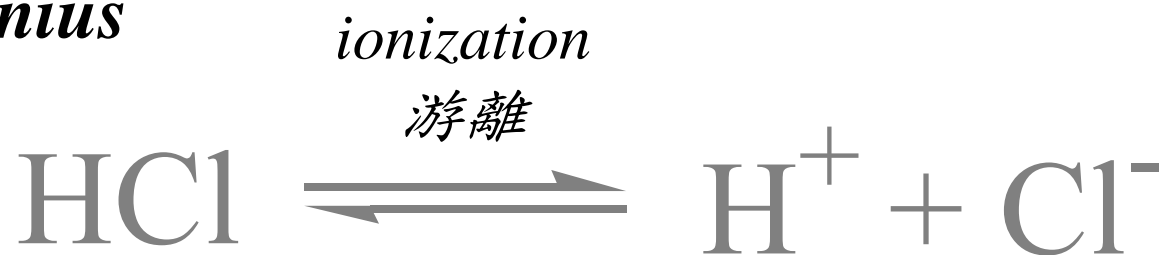
共軛酸鹼對酸是相互競爭

■ *Chemical equilibrium for acid-base reactions*

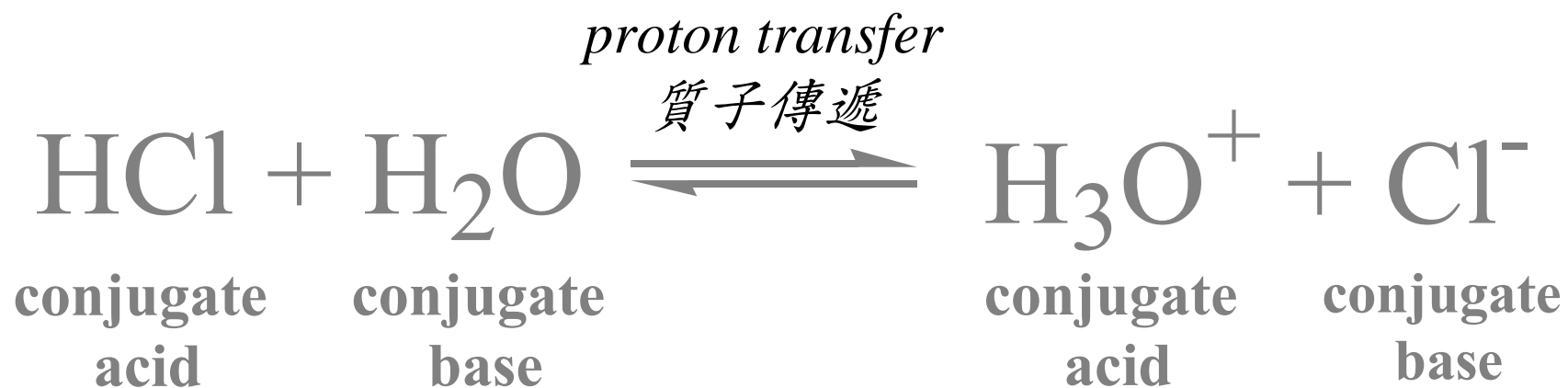
酸鹼反應是共軛酸鹼對的化學平衡，反應傾向從強共軛酸鹼往弱共軛酸鹼的方向進行

● *Arrhenius vs Brønsted-Lowry concepts*

Arrhenius



Brønsted-Lowry



● *Self- Ionization of Water*

水的自身游離

- *The chemistry of aqueous solution is unique*
水溶液有獨特的化學行為
- *Rapid proton exchange via H-bonding*
水分子間藉由氫鍵進行快速的質子交換
- *H_3O^+ is hydrated proton, and called hydronium ion*
質子在水溶液中呈水合的狀態稱為銜離子(H_3O^+)
- *Actually, either H^+ or OH^- is hydrated*
事實上，大部分溶在水中的物質都是呈水合的狀態

- **Self ionization of water is in chemical equilibrium**
水的自身游離常呈化學平衡狀態



$$K = \frac{[\text{H}^+][\text{OH}^-]}{[\text{H}_2\text{O}]}$$

- $K_w = [\text{H}_3\text{O}^+][\text{OH}^-]$, *and is called ion product constant*
 $K_w = [\text{H}_3\text{O}^+][\text{OH}^-]$, 稱為離子積常數
- At 25°C, $[\text{H}_3\text{O}^+] = [\text{OH}^-] = 1.0 \times 10^{-7} \text{ M}$; $K_w = 1.0 \times 10^{-14}$

● *Acid-Base in Other Solutions*

其他溶液中的酸鹼平衡

■ *in ethanol 乙醇中*



- *Ethoxide is a stronger base than water, and protonated ethanol is a stronger acid than water.*

乙烷氧離子在水中是強鹼，質子化的乙醇則是強酸

- *Basicity: $\text{EtO}^- > \text{OH}^- > \text{H}_2\text{O} > \text{EtOH} > \text{H}_3\text{O}^+ > \text{EtOH}_2^+$*

■ *in ammonia* 氨水中

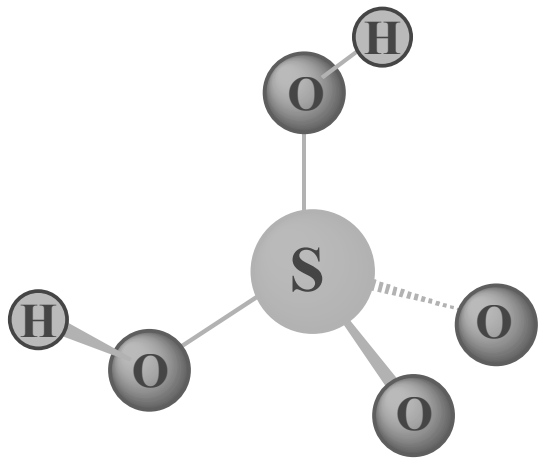


■ ***Bacicity:*** $\text{NH}_2^- > \text{OH}^- > \text{NH}_3 > \text{H}_2\text{O} > \text{NH}_4^+ > \text{H}_3\text{O}^+$



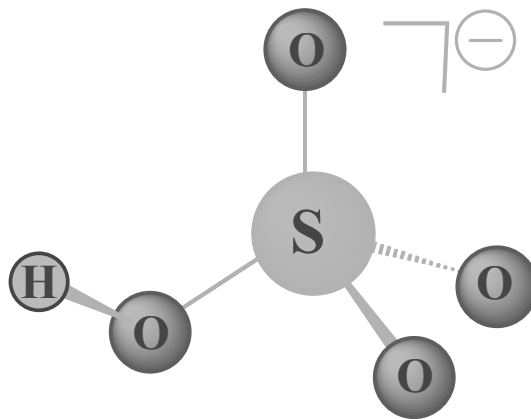
Structure of Oxyacids

常見含氧酸的分子結構



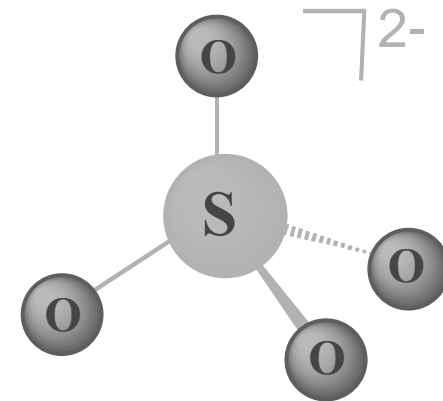
sulfuric acid

硫酸



hydrogen sulfate

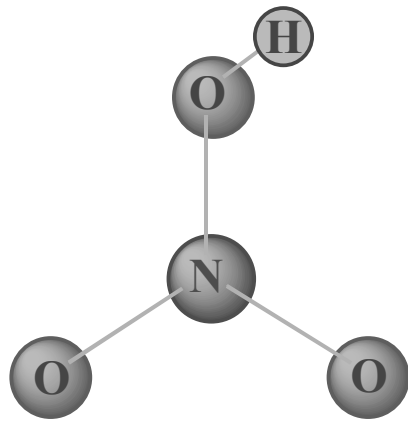
硫酸氫根



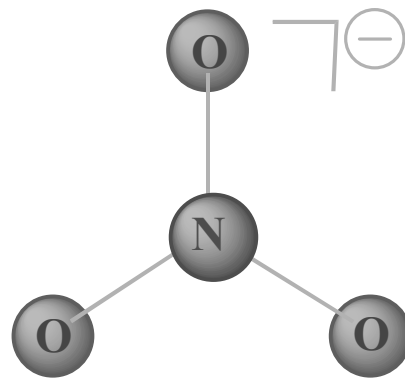
sulfate (tetrahedral)

硫酸根(正四面體)

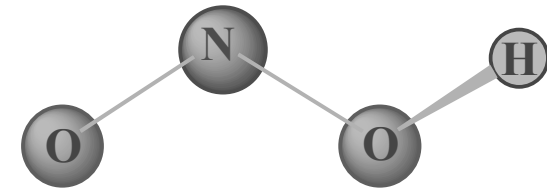
The higher oxidation state of the central atom, the stronger acid it will be. 中央原子的氧化態越高的酸酸性愈強



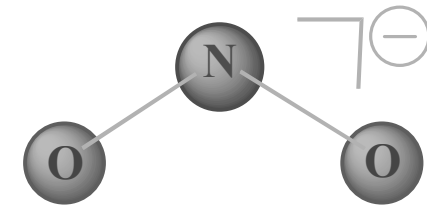
nitric acid
硝酸



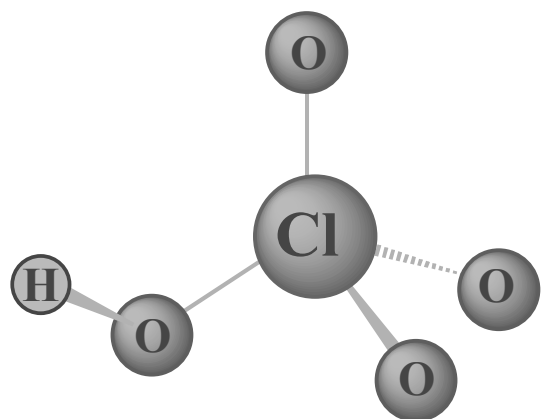
nitrate
(trigonal planar)
硝酸根(平面三角形)



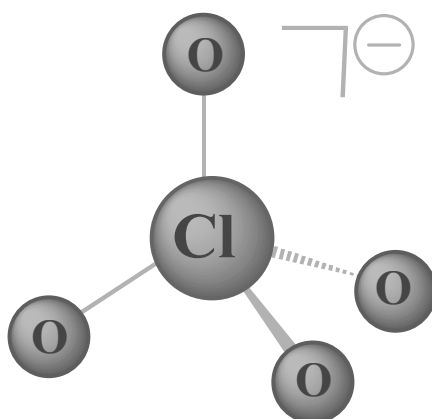
nitrous acid
亞硝酸



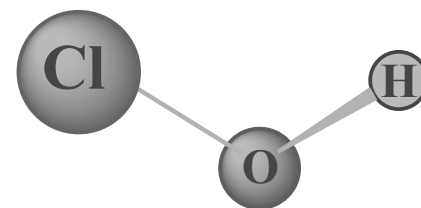
nitrite (angular)
亞硝酸根(角形)



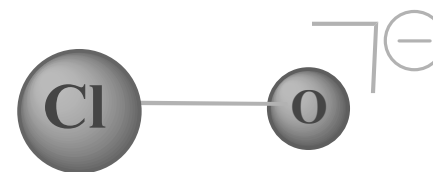
perchloric acid
過氯酸



perchlorate
(tetrahedral)
過氯酸根(正四面體)



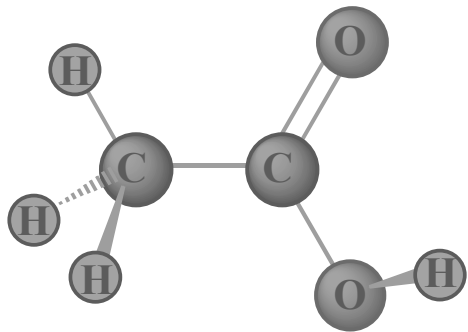
hypochlorous acid
次氯酸



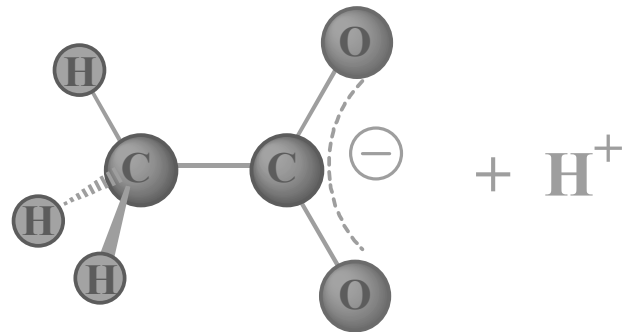
hypochlorite (linear)
次氯酸根



Organic Acids 有機酸

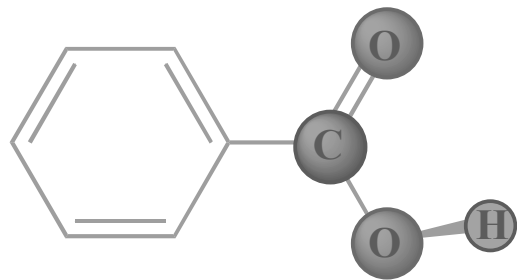


acetic acid 醋酸

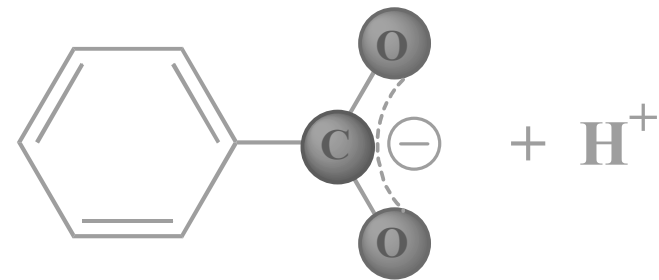


acetate

醋酸根



benzoic acid 苯酸



benzoate

苯酸根

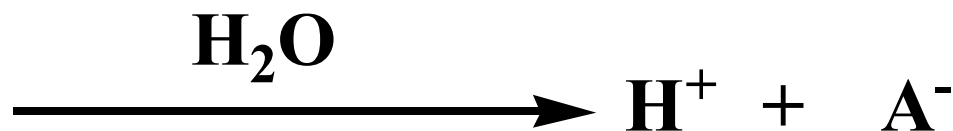
● *Acid Strength 酸的強度*

- K_a — *acid dissociation constant, indicating the extent of dissociation of acids* K_a 是酸的解離常數
- *the equilibrium of strong acid goes toward its complete dissociation* 強酸完全解離
- *the weak acid reaches its equilibrium with partial dissociation* 弱酸部分解離
- $pH = -\log [H^+]$
- *the pH scale of aqueous solutions is <14*
水溶液的pH值範圍<14
- *pH meter —Saturated Calomel Electrode (SCE)*
$$Hg + Cl^- = \frac{1}{2} Hg_2Cl_2 + e^-$$

● *Acid Strength*

■ *pH of strong acid, $[H^+] = [HA]_0$*

■ *Leveling Effect 平準效應*



All strong acids or bases show the same strength in the same solvent. In aqueous solution, the strongest acid allowed is H^+ , the strongest base allowed is OH^- .

水中的最強酸是 H^+ ，最強鹼是 OH^-

● *Acid Strength*

■ *pH of weak acid,*



before $[\text{HA}]_0$

after $[\text{HA}]_0 - x$ x x

$$K_a = \frac{x^2}{[\text{HA}]_0 - x} \quad [\text{HA}]_0 \gg x,$$
$$x = [\text{H}^+] = (K_a [\text{HA}]_0)^{1/2}$$

● *Percent Dissociation* 解離率

$$\frac{x}{[HA]_0} \times 100\% = \frac{\sqrt{K_a [HA]_0}}{[HA]_0} \times 100\%$$

$$= \sqrt{\frac{K_a}{[HA]_0}} \times 100\%$$

● *Percent Dissociation* 計算解離率



before C

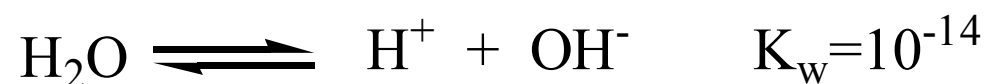
after C- α C α C α C

$$K_{\alpha} = \frac{\alpha^2 C^2}{C - \alpha C} = \frac{\alpha^2 C^2}{C(1 - \alpha)} = \frac{C\alpha^2}{(1 - \alpha)}$$

$$\therefore \frac{\alpha^2}{1 - \alpha} = \frac{K_{\alpha}}{C} \quad \alpha \ll 1 \quad \alpha = \sqrt{\frac{K_a}{C}}$$

● *The pH of mixture of weak acids depends on the relative acidity*

Example: Calculate the pH of a solution that contains 1.00 M HCN (6.2×10^{-10}) and 5.00 M HNO_2 (4.0×10^{-4}) and calculate $[\text{NO}_2^-]$ and $[\text{CN}^-]$.



Nitrous acid is stronger than cyanic acid to the 6th order of magnitude, it will dominate $[\text{H}^+]$.

$$4.0 \times 10^{-4} = \frac{[\text{H}^+][\text{NO}_2^-]}{[\text{HNO}_2]} = \frac{[\text{H}^+]^2}{5.00 - [\text{H}^+]} \approx \frac{[\text{H}^+]^2}{5.00}$$

$$[\text{H}^+] = [\text{NO}_2^-] = 4.5 \times 10^{-2} \text{ M} \quad \text{pH} = 1.35$$

$$6.2 \times 10^{-10} = \frac{[\text{H}^+][\text{CN}^-]}{[\text{HCN}]} \approx \frac{(4.5 \times 10^{-2})[\text{CN}^-]}{1.00}$$

$$\therefore [\text{CN}^-] = 1.4 \times 10^{-8} \text{ M}$$

The dissociation of cyanic acid is suppressed by nitrous acid.

● ***The pH of very dilute acid*** ($[H^+] < 1.0 \times 10^{-6} M$)



$$K_a = \frac{[H^+][A^-]}{[HA]} \quad \dots\dots(\text{eq 1})$$



$$K_w = [H^+][OH^-] = 1.0 \times 10^{-14} \quad \dots\dots(\text{eq 2})$$

mass balance: $[HA]_0 = [HA] + [A^-] \quad \dots\dots(\text{eq 3})$

質量平衡

charge balance: $[H^+] = [OH^-] + [A^-] \quad \dots\dots(\text{eq 4})$

電荷平衡

Unknowns: $[H^+], [OH^-], [HA], [A^-]$

Knowns: $[HA]_0, K_a, K_w$

$$[\text{H}^+] = [\text{A}^-] + [\text{OH}^-]$$

$$= [\text{A}^-] + \frac{K_w}{[\text{H}^+]}$$

$$\therefore [\text{A}^-] = [\text{H}^+] - \frac{K_w}{[\text{H}^+]}$$

$$[\text{HA}] = [\text{HA}]_0 - [\text{A}^-]$$

$$= [\text{HA}]_0 - \left([\text{H}^+] - \frac{K_w}{[\text{H}^+]}\right)$$

$$K_a = \frac{[\text{H}^+] \left([\text{H}^+] - \frac{K_w}{[\text{H}^+]}\right)}{[\text{HA}]_0 - \left([\text{H}^+] - \frac{K_w}{[\text{H}^+]}\right)} = \frac{[\text{H}^+]^2 - K_w}{[\text{HA}]_0 - \left(\frac{[\text{H}^+]^2 - K_w}{[\text{H}^+]}\right)}$$

$$\text{if } [\text{H}^+]^2 \gg K_w \quad K_a = \frac{[\text{H}^+]^2}{[\text{HA}]_0 - [\text{H}^+]}$$

$$\text{if } [\text{HA}]_0 \gg ([\text{H}^+]^2 - K_w)/[\text{H}^+] \quad [\text{H}^+] = (K_a[\text{HA}]_0 + K_w)^{1/2}$$

● *learn how to set up equations*

會設定方程式

● *learn mass and charge balance*

會使用質量及電荷平衡的概念

● *learn how to solve the unknowns*

找出未知量的參數

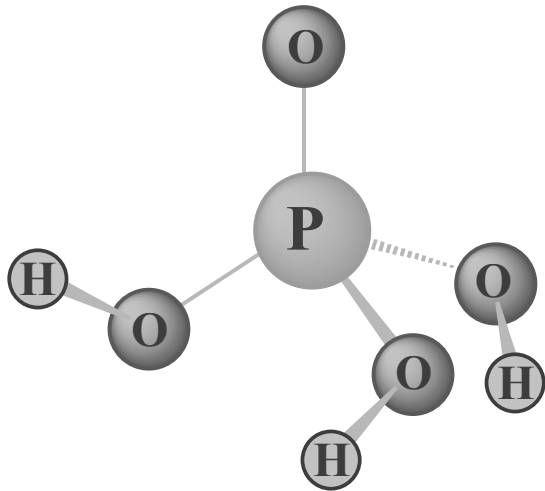
● *learn how to do approximation*

使用概算法簡化計算

● *learn the meaning of approximation*

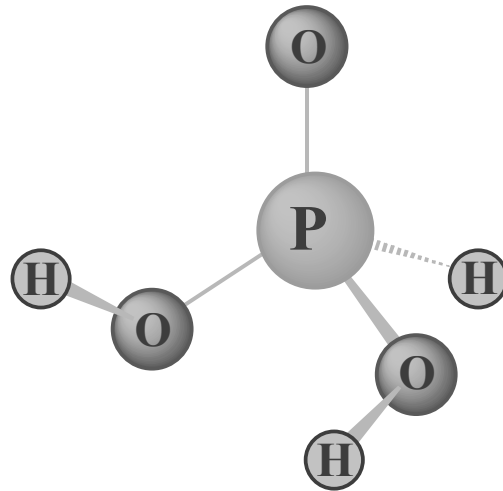
檢驗概算的假設

● *Polyprotic (Polybasic) Acids* 多質子酸



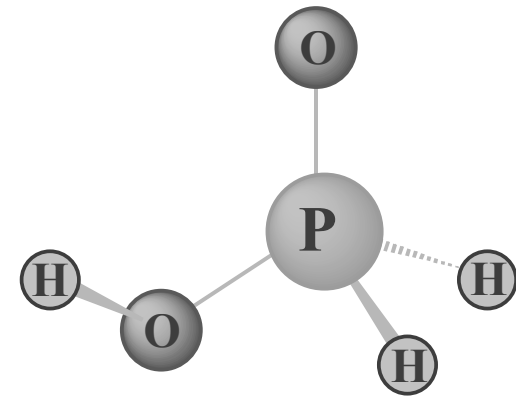
phosphoric acid
(tribasic)

磷酸(三質子酸)



phosphorous acid
(dibasic)

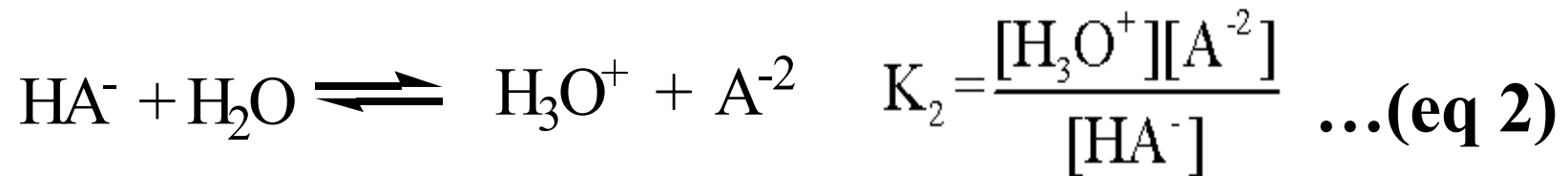
亞磷酸(二質子酸)



hypophosphorous acid
(monobasic)

次磷酸(單質子酸)

● *The pH of a diprotic acid – H₂CO₃*



mass balance:

$$C_{\text{H}_2\text{A}} = [\text{H}_2\text{A}] + [\text{HA}^-] + [\text{A}^{2-}] \dots\dots(\text{eq 3})$$

charge balance:

$$[\text{H}_3\text{O}^+] = [\text{OH}^-] + [\text{HA}^-] + 2[\text{A}^{2-}] \dots\dots(\text{eq 4})$$

Unknowns: $[\text{H}^+]$, $[\text{OH}^-]$, $[\text{H}_2\text{A}]$, $[\text{HA}^-]$, $[\text{A}^{2-}]$

Knowns: $C_{\text{H}_2\text{A}}$, K_1 , K_2 , K_w

if $K_1 \gg K_2$ (more than 1000 fold larger)

$$[HA^-] \gg [A^{2-}]$$

$$[H_3O^+] \approx [HA^-]$$

$$[A^{2-}] \approx K_2 \text{ (double checked later)}$$

$$[H_2A] = [H_2A] + [HA^-] = [H_2A] + [H_3O^+]$$

$$K_1 = \frac{[H_3O^+]^2}{C_{H_2A} - [H_3O^+]}$$

$$\text{if } C_{H_2A} \gg [H_3O^+]$$

$$[H_3O^+] = \sqrt{K_1 C_{H_2A}}$$

Calculate pH of 5.00 M H₃PO₄ and the concentrations of anions.



$$K_{a_1} = 7.5 \times 10^{-3} = \frac{[\text{H}^+][\text{H}_2\text{PO}_4^-]}{[\text{H}_3\text{PO}_4]} \approx \frac{x^2}{5.0}$$

$$[\text{H}^+] = 1.9 \times 10^{-1} \quad \text{pH} = 0.72$$

$$K_{a_2} = 6.2 \times 10^{-8} = \frac{[\text{H}^+][\text{HPO}_4^{2-}]}{[\text{H}_2\text{PO}_4^-]}$$

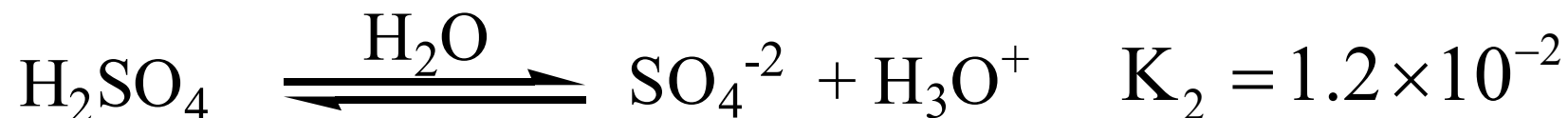
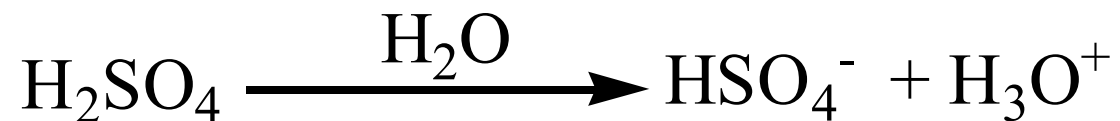
$$[\text{H}^+] \approx [\text{H}_2\text{PO}_4^-]$$

$$\therefore [\text{HPO}_4^{2-}] \approx K_{a_2} = 6.2 \times 10^{-8}$$

$$K_{a_3} = 4.8 \times 10^{-13} = \frac{[\text{H}^+][\text{PO}_4^{3-}]}{[\text{HPO}_4^{2-}]} = \frac{0.19[\text{PO}_4^{3-}]}{6.2 \times 10^{-8}}$$

$$\therefore [\text{PO}_4^{3-}] = 1.6 \times 10^{-19} \text{ M}$$

Calculate $[H_3O^+]$ for 0.0100 M H_2SO_4 .



$[H_3O^+] \approx [HSO_4^-] = 0.0100 \text{ M}$ approximation

$$\frac{[H_3O^+][SO_4^{2-}]}{[HSO_4^-]} \approx [SO_4^{2-}] = 1.2 \times 10^{-2} \text{ M}$$

$[SO_4^{2-}] \ll [HSO_4^-]$ or $[SO_4^{2-}] \ll [H_3O^+]$ thus is not a proper assumption.

$$C_{\text{H}_2\text{SO}_4} = [\text{HSO}_4^-] + [\text{SO}_4^{2-}] \quad \dots \text{Mass balance}$$

$$[\text{H}_3\text{O}^+] = [\text{HSO}_4^-] + 2[\text{SO}_4^{2-}] \quad \dots \text{charge balance}$$

$$[\text{H}_3\text{O}^+] - C_{\text{H}_2\text{SO}_4} = [\text{SO}_4^{2-}]$$

$$[\text{H}_3\text{O}^+] = 0.0100 + [\text{SO}_4^{2-}]$$

$$[\text{HSO}_4^-] = 0.0100 - [\text{SO}_4^{2-}]$$

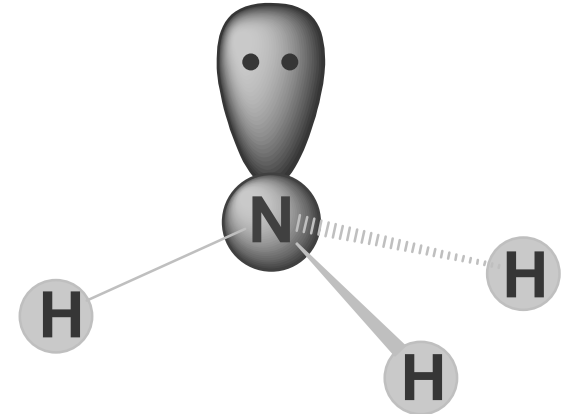
$$K_2 = \frac{[\text{H}_3\text{O}^+][\text{SO}_4^{2-}]}{[\text{HSO}_4^-]} = \frac{(0.0100 + [\text{SO}_4^{2-}])([\text{SO}_4^{2-}])}{(0.0100 - [\text{SO}_4^{2-}])}$$

$$[\text{SO}_4^{2-}] = 4.5 \times 10^{-3} \text{ M}$$

$$[\text{H}_3\text{O}^+] = 0.0145 \text{ M}$$

$$[\text{HSO}_4^-] = 0.0055 \text{ M}$$

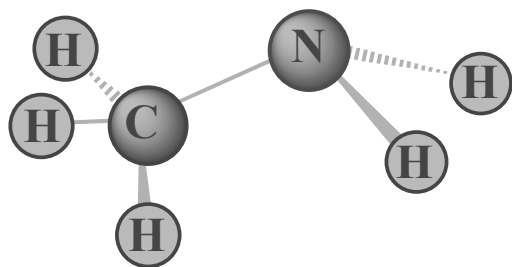
● *Inorganic Bases* 無機鹼



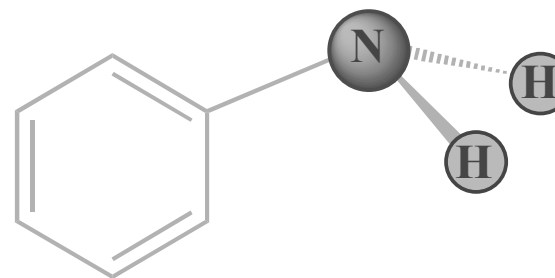
- *ammonia* 氨
- *metal hydroxides* 金屬氫氧化物: NaOH , KOH , Ca(OH)_2
- *metal oxides* 金屬氧化物: CaO , BaO
- *metal hydrides* 金屬氫化物: NaH , KH
- *metal amides* 金屬氮化物: NaNH_2 , LiNMe_2 , NaOMe
- *weak acid salts* 金屬弱酸鹽: NaOAc , NaCN , Na_2CO_3

● *Organic amines* 有機鹼

■ *primary (1°) amine* 一級胺



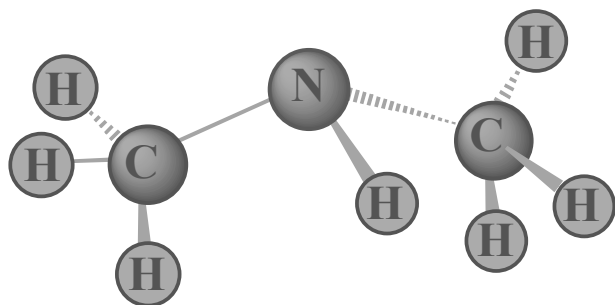
methyl amine
甲胺



aniline
苯胺

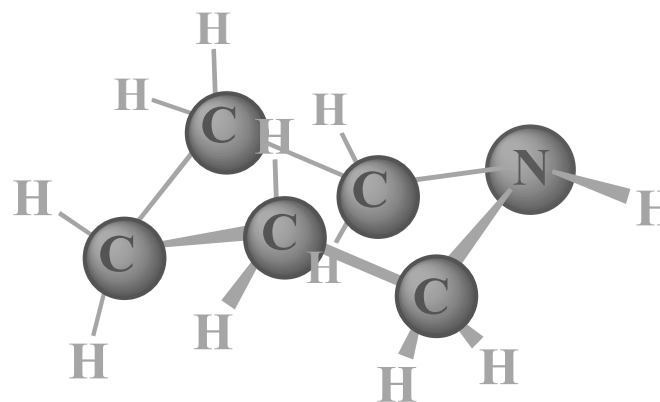
● *Organic amines*

■ *secondary (2°) amine* 二級胺



dimethyl amine

二乙胺

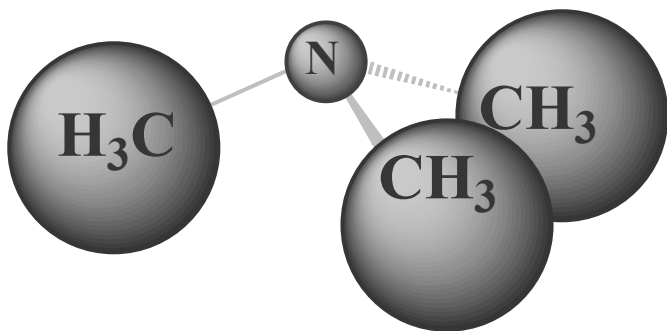


piperidine

環戊胺

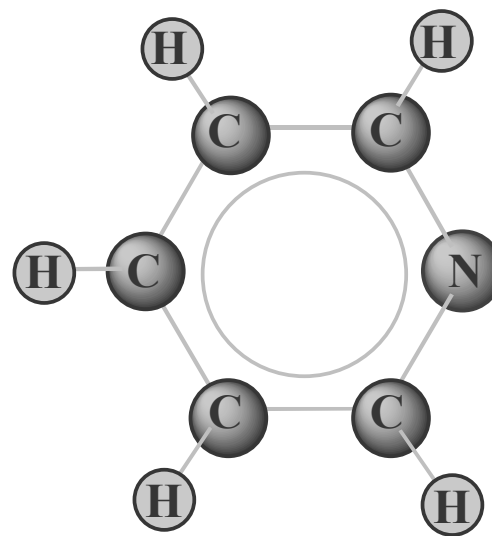
● *Organic amines*

■ *tertiary (3°) amine* 三級胺



trimethyl amine

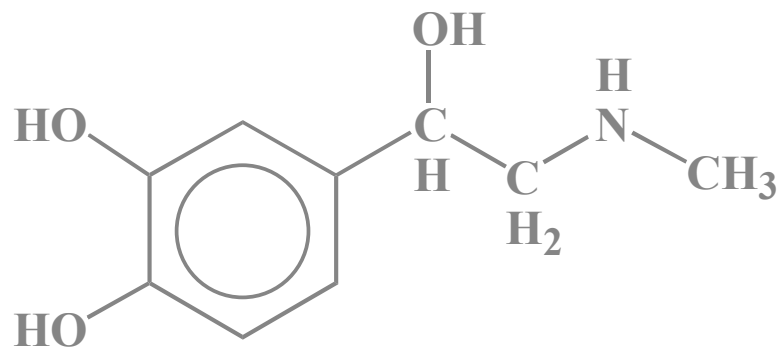
三甲胺



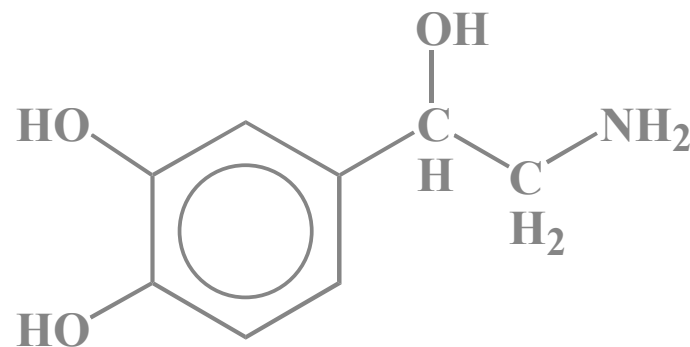
Pyridine

吡啶

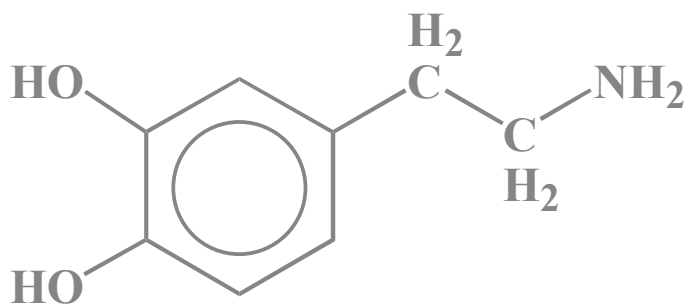
● *Biofunctional amines* 生物胺



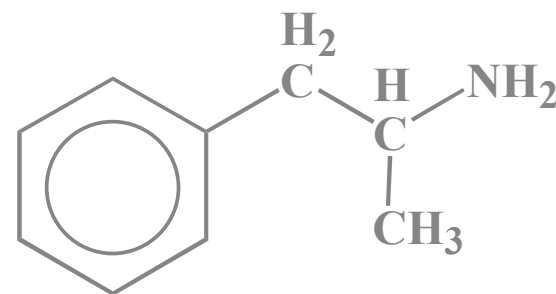
Epinephrine
腎上腺素



Norepinephrine
降腎上腺素



dopamine
多巴胺



amphetamine
安非他命

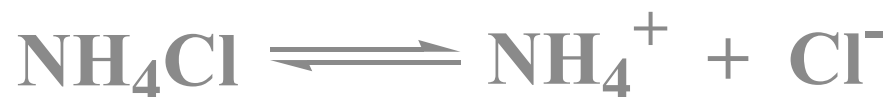
● *Salts* 鹽類

- *Neutral Salts: salts formed from strong acid & strong base are always of neutral salts, pH = 7.*
強酸與強鹼形成的鹽為中性鹽

Example:



- **Acidic Salts: salts formed from strong acid & weak base** 強酸與弱鹼形成酸性鹽



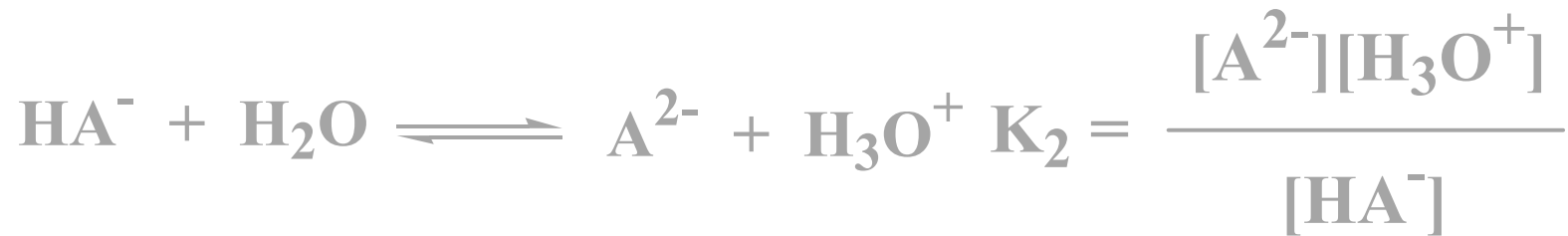
$$K_a = \frac{[\text{NH}_3][\text{H}_3\text{O}^+]}{[\text{NH}_4^+]} \sim \frac{[\text{H}_3\text{O}^+]^2}{[\text{NH}_4^+]}$$

For 1M NH₄Cl at 25 °C

$$\begin{aligned} [\text{H}_3\text{O}^+] &= (K_a[\text{NH}_4^+])^{1/2} = (K_a[\text{NH}_4\text{Cl}])^{1/2} \\ &= 2.4 \times 10^{-5} \text{ M} \end{aligned}$$

∴ pH=4.6 The solution is slightly acidic.

■ *Solution of acidic salts of ampholyte* 兩性鹽



Mass balance: $C_{\text{NaHA}} = [\text{H}_2\text{A}] + [\text{HA}^-] + [\text{A}^{2-}]$

Charge balance: $[\text{Na}^+] + [\text{H}_3\text{O}^+] = [\text{OH}^-] + [\text{HA}^-] + 2[\text{A}^{2-}]$

$$[\text{H}_2\text{A}] = [\text{A}^{2-}] + [\text{OH}^-] - [\text{H}_3\text{O}^+]$$

$$\frac{K_w [HA^-]}{K_1 [OH^-]} = \frac{K_2 [HA^-]}{[H_3O^+]} + [OH^-] - [H_3O^+]$$

$$\frac{[H_3O^+][HA^-]}{K_1} = \frac{K_2 [HA^-]}{[H_3O^+]} + \frac{K_w}{[H_3O^+]} - [H_3O^+]$$

$$[H_3O^+]^2 \left(\frac{[HA^-]}{K_1} + 1 \right) = K_2 [HA^-] + K_w$$

$$[H_3O^+] = \sqrt{\frac{K_1 K_2 [HA^-] + K_1 K_w}{[HA^-] + K_1}}$$

if both K_1 , K_2 are small

$$[HA^-] \approx C_{NaHA}$$

$$\text{and } K_1 \ll [HA^-] = C_{NaHA}$$

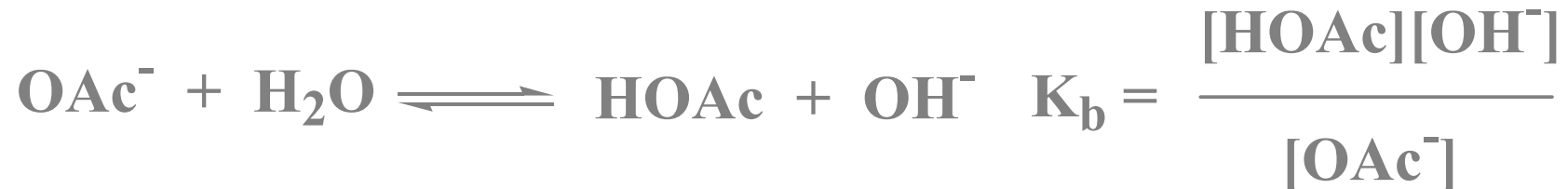
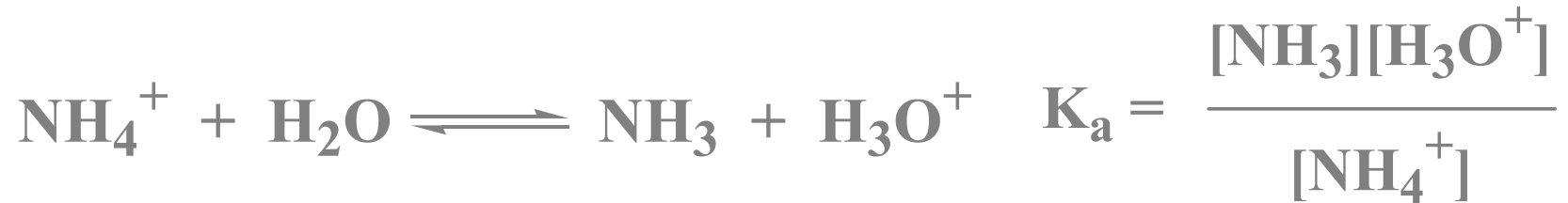
$$K_w \ll C_{NaHA}$$

$$[H_3O^+] = \sqrt{K_1 K_2}$$

$$pH = \frac{1}{2} pK_1 + \frac{1}{2} pK_2$$

■ Salts formed from weak acid & weak base (NH_4OAc)

弱酸與弱鹼形成的鹽



Mass balance:

$$C_{\text{NH}_4\text{OAc}} = [\text{NH}_4^+] + [\text{NH}_3] = [\text{HOAc}] + [\text{OAc}^-]$$

Charge balance:

$$[\text{NH}_4^+] + [\text{H}_3\text{O}^+] = [\text{OH}^-] + [\text{OAc}^-]$$

$$[\text{NH}_3] - [\text{H}_3\text{O}^+] = [\text{HOAc}] - [\text{OH}^-]$$

$$\frac{[\text{NH}_4^+]}{[\text{H}_3\text{O}^+]} \frac{K_w}{K_b} - [\text{H}_3\text{O}^+] = \frac{[\text{OAc}^-][\text{H}_3\text{O}^+]}{K_a} - \frac{K_w}{[\text{H}_3\text{O}^+]}$$

⇓

$$[\text{NH}_4^+] \frac{K_w}{K_b} - [\text{H}_3\text{O}^+]^2 = \frac{[\text{OAc}^-][\text{H}_3\text{O}^+]^2}{K_a} - K_w$$

⇓

$$\left(1 + \frac{[\text{OAc}^-]}{K_a}\right) [\text{H}_3\text{O}^+]^2 = [\text{NH}_4^+] \frac{K_w}{K_b} + K_w$$

⇓

$$[\text{H}_3\text{O}^+] = \sqrt{\frac{K_w K_a ([\text{NH}_4^+] + K_b)}{K_b (K_a + [\text{OAc}^-])}}$$

K_a, K_b are small, $\therefore [\text{NH}_4^+] = [\text{OAc}^-] \approx F_{\text{NH}_4\text{OAc}}$

$$\therefore [\text{H}_3\text{O}^+] = \sqrt{\frac{K_w K_a}{K_b}}$$

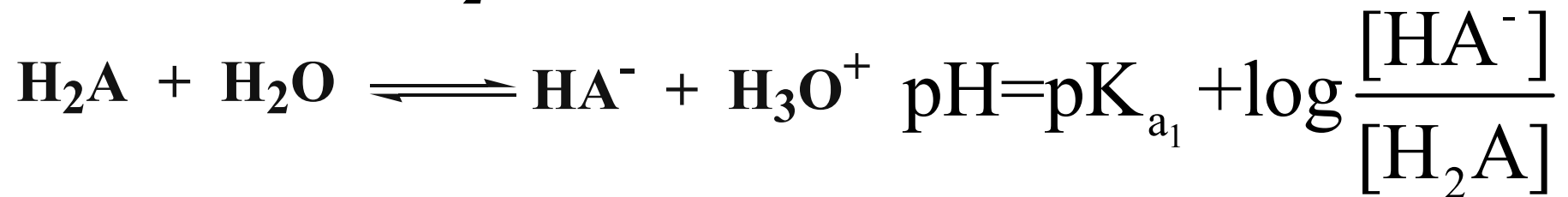
if $K_a > K_b$ soln is acidic

$K_a < K_b$ soln is basic

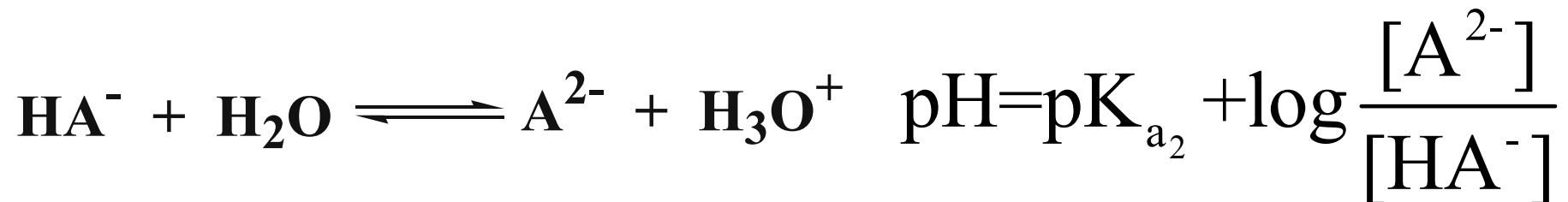
$K_a = K_b$ soln is neutral

■ Solution of weak acid & Its Salt

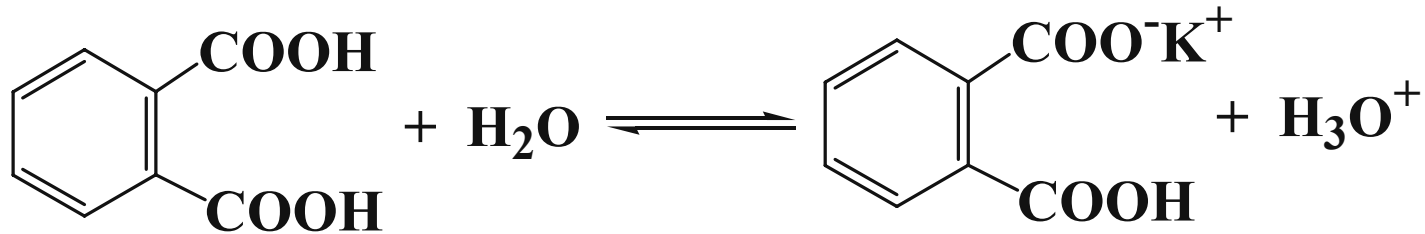
弱酸及其鹽類的同離子效應



or



■ ***0.0100 M phthalic acid/0.200 M KHP***



$$K_1 = \frac{[\text{HP}^-][\text{H}_3\text{O}^+]}{[\text{H}_2\text{P}]} = 1.3 \times 10^{-3}$$

$$K_2 = \frac{[\text{P}^{2-}][\text{H}_3\text{O}^+]}{[\text{HP}^-]} = 3.9 \times 10^{-6} \ll K_1$$

$$[\text{H}_2\text{P}] = 0.100 - [\text{H}_3\text{O}^+] \approx 0.100 \text{ M}$$

$$[\text{HP}^-] = 0.200 - [\text{H}_3\text{O}^+] \approx 0.200$$

■ **Method 1.**

$$\frac{0.200[\text{H}_3\text{O}^+]}{0.100} = 1.3 \times 10^{-3}$$

$$[\text{H}_3\text{O}^+] = 6.5 \times 10^{-4} \text{ M} \quad \text{pH} = 3.19$$

■ **Method 2.**

$$\text{pH} = \text{pK}_{a_1} + \log\left(\frac{[\text{HA}^-]}{[\text{H}_2\text{P}]}\right)$$

$$= 2.89 + \log\frac{0.2}{0.1}$$

$$= 3.19$$

總結

酸、鹼、鹽都是在水中會游離的物質，水會發生自身解離，所以酸與鹼都會和水分子競爭質子，鹽類則發生水合的行為。

不同的物質解離程度和競爭質子的能力均不同，利用測量酸、鹼、鹽在水中的平衡的情形，可以計算各種化學成分在水溶液中的含量。

有機、無機與生化物質都可能在水中有酸鹼鹽的性質。物質的結構與組成都影響其酸或鹼的性質。